Tracking decision makers under uncertainty

Amos Arieli
Department of Neurobiology, the Weizmann Institute of Science

Yaniv Ben-Ami
School of Economics, Tel Aviv University

Ariel Rubinstein
University of Tel Aviv Cafes,
School of Economics, Tel Aviv University and
Department of Economics, New York University

Abstract:
Eye tracking is used to investigate human choice procedures. We infer from eye movement patterns in choice problems where the deliberation process is clear to deliberations in problems of choice between two lotteries. The results indicate that participants tend to compare prizes and probabilities separately. The data provide little support for the hypothesis that decision makers use an expected utility type of calculation exclusively. This is particularly true when the calculations involved in comparing the lotteries are complicated.

Key-words: Decision Making, Expected Utility, Eye tracking, Neuroeconomics, Similarity.

Acknowledgements
We wish to thank Ayala Arad, Paul Glimcher, Ori Heffetz, Rosemarie Nagel, Doron Ravid and Dan Zeltzer for their valuable comments. We acknowledge support from the Israeli Science Foundation (grant 259/08).
1. Introduction

How do people choose between lottery 1 which yields the prize $x_1$ with probability $p_1$ and lottery 2 which yields the prize $x_2$ with probability $p_2$? There are two types of procedure that come to mind:

**Holistic (H-) procedures:** In this type of procedure, the decision maker treats the alternatives holistically. For example, he evaluates the certainty equivalent of each of the alternatives and chooses the one with the higher certainty equivalence. Or, he computes the expectation of each of the two lotteries and chooses the one with the higher expectation. More generally, he might have functions $g$ and $v$ in mind and choose the lottery with the higher $g(p_i)v(x_i)$. A canonical formula for such a procedure would assume the existence of a function $u$ such that lottery 1 is chosen if $u(x_1,p_1) > u(x_2,p_2)$.

**Component (C-) procedures:** The decision maker compares prizes and probabilities separately. In the case that one of the lotteries yields a larger prize with a higher probability he will choose that lottery. Otherwise, he checks for similarity between the prizes and between the probabilities and uses that similarity to make the choice. If, for example, the prize $x_1$ is much larger than the prize $x_2$ and the probabilities are similar, even though $p_2$ is higher than $p_1$, he would choose lottery 1. A canonical procedure of this type would assume the existence of functions $f$, $g$ and $h$, such that lottery 1 is chosen if $h(f(x_1, x_2), g(p_1, p_2)) > 0$. The idea that the choice of an alternative is based, at least partially, on a comparison of components has appeared in the psychological literature (see, for example, Tversky, Sattath and Slovik (1988)).

Our research is motivated by the bounded rationality approach to decision making which focuses on the choice procedures used by individuals. The classical economic approach attempted to explain choice behavior using only the observed choices. Contemporary research (especially in Psychology and Neuroeconomics) attempts to elicit information about choice procedures from observations of the decision maker during his deliberations (including, for example, eye movements and activity in various areas of the brain).

Whereas evidence for H-procedures supports theories that describe the decision maker as explicitly maximizing a utility function, evidence for C-procedures opens the door to other models (such as the one described in Rubinstein (1988)) which require an explicit comparison of components and are not necessarily consistent with maximization of a well-defined preference.
relation. In this paper, we go no further than examining experimental data to find evidence for the use of C-procedures. We believe that experimental evidence as to how people choose between lotteries may change the way in which decision making under uncertainty is modeled; however, as always, the proof is in the pudding.

We attempt to uncover procedures used by decision makers by following their eye-movements while they deliberate over a choice. This method was first used in research done in the 70s and was recently revisited.¹ Eye tracking complements another interesting approach which observes mouse movements using a program called MouseLab (see Payne et al. (1993)). In this approach, the participant accesses the information hidden behind boxes on the computer screen by moving the cursor over the boxes.² Particularly relevant for our purposes is Johnson, Schulte-Mecklenbeck and Willemsen (2008) who used MouseLab techniques to study the choice between gambling procedures. Both methods are attractive in that they are cheap to use and produce data that is straightforward to interpret (in contrast to methods that record signals from the brain). However, eye tracking has an advantage over MouseLab in that it records natural and unconscious movements while the need to move the mouse in MouseLab requires a somewhat less natural information acquisition strategy (see Lohse and Johnson (1996)).

2. The Research Concept

In our study, participants³ were asked to respond to a sequence of simple virtual choice problems. The participants were paid only a show-up fee of $12. Participants were not paid for

---


² The site http://www.mouselabweb.org demonstrates the program and allows one to try it out.

³ The participants (24 males and 23 females; average age of 27) all had normal or corrected-to-normal vision and were students (in fields other than economics) in Rehovot, Israel. Participants signed an informed consent form in accordance with the Declaration of Helsinki.
choices made. There is ample evidence that the lack of monetary incentives does not significantly affect subjects’ choices (see Camerer and Hogarth (1997)). In any case, note that we are interested only in the choice process that led participants to make their particular choices and not in the choice distributions themselves, which are reported only for the sake of completeness.

In each problem, a participant was asked to choose between two alternatives, Left (L) and Right (R), by clicking on the mouse. Each decision problem was presented on a separate screen (Figure 1), in which two parameters, a and b, describe the L alternative and two parameters, c and d, describe the R alternative.

![Figure 1: Schematic representation of the screen shown to the participants.](image)

No time restrictions were imposed on the participants and a typical median response time was eight seconds.

Our focus is on the case in which L is a lottery that yields $a with probability b (and $0 with probability 1-b) and R is the lottery yielding $c with probability d (see Figure 2).

![Figure 2: Scheme for choice under uncertainty problems.](image)

---

4 We did not alternate the sides on which the alternatives are presented. In order to check whether presenting alternatives on the left side (white letters) or on the right side (black letters) makes any difference, we calculated the distribution of response time over all the problems for participants who chose L (N=902) and participants who chose R (N=805). We found that the average response times of the two groups were practically identical (5.81 sec and 5.75 sec; T-test p-value of 42.5%).
We concentrate on comparing the intensity of horizontal and vertical eye movements. Our hypothesis is that decision makers who follow H-procedures will show intensive vertical eye movements while decision makers who follow C-procedures will show intensive horizontal eye movements.

3. The Method

An eye-tracking system was used in order to continuously record a subject’s point of gaze. Analyzing the huge amount of recorded data was not straightforward. We first transformed it into movies showing the path of eye movement on the screen. However, there were only a few cases in which the choice procedure was discernable from the movie (a sample movie can be watched at http://arielrubinstein.tau.ac.il/ABR09/). Thus, we needed to develop a measure of the intensity of horizontal and vertical movements.

We divided the screen into four quarters: Top Left, Top Right, Bottom Left and Bottom Right. Eye movements between two sections of the screen are classified into six categories: Left-Vertical, Right-Vertical, Top-Horizontal, Bottom-Horizontal, Descending-Diagonal and Ascending-Diagonal. For each problem and each participant, we calculated the proportion of time spent in each of the six categories of eye movements. Averaging over all participants produced a vector \( \alpha \) on which our analysis is based. \(^6\) (The six components of \( \alpha \) sum up to 100%).

---

5 We used a high-speed eye-tracking system (iView) made by SensoMotoric Instruments (SMI) which is based on an infrared light camera. It captures (at a sampling frequency of 240Hz or one sample every 4.2 milliseconds) a high-resolution image of the pupil and corneal reflection.

6 Given a choice problem, the exact calculation of the vector \( \alpha \) is done as follows:
(i) For each participant \( i \), let \( \theta \) be the point in time at which the problem is first presented and \( T \) be the point in time at which the participant clicked on the mouse.
(ii) Denote the transition times between sections of the screen by: \( t_1, t_2, \ldots, t_k, \ldots, t_n \).
(iii) Divide the segment of time \([0, T]\) into \( n \) intervals: \([0, (t_1 + t_2)/2], [(t_1 + t_2)/2, (t_2 + t_3)/2], \ldots, [(t_{n-1} + t_n)/2, T]\). Credit the duration of the \( k \)'th interval \((k=1,..,n)\) to the total for the type of eye movement that occurred at \( t_k \).
(iv) Divide the time credited to each type of eye movement by the total of all the eye movements to obtain a vector \( \alpha(i) \) (for participant \( i \)), which consists of six numbers representing the proportion of time spent in each type of movement.
(v) Average the vectors \( \alpha(i) \) over all participants. Denote the vector of averages as \( \alpha \).
We omitted any period of time for which the eye tracker did not identify the eye position, which was usually the result of blinking. In addition, in order to identify diagonal movements, which always pass briefly through another section of the screen, we omitted any period of time in which the participant's gaze stayed in a particular section for less than 100 msec. Cases in which the above omissions exceeded 20% of the response time were excluded from the sample.7

High $\alpha$-values for the two vertical eye movements will imply that participants’ choices were largely based on relating to each alternative as a unit and comparing them as such. High $\alpha$-values for the horizontal eye movements will indicate that participants based their decisions heavily on comparing each of the features of the alternatives separately.

We suspected that the $\alpha$-values are sensitive to variation in the level of difficulty in understanding the question's parameters (e.g., if one of the parameters takes a long time to read, this will lengthen the duration of the movement into and out of that section of the screen). Therefore, we also produced a similar vector $\beta$ for the number of transitions in each type of eye movement. We found that the two measures produced almost identical results.8

4. Results

The basic results are presented in Table 1, which shows the $\alpha$-values in four lottery choice problems.

---

7 The same subjects responded to all of the problems. However, due to the need to eliminate answers for which the recorded data was not complete, the subset of participants for analysis differs somewhat from one question to the next.

8 Russo and Rosen (1975) and Russo and Dosher (1983) based their analysis on counting movements from one section of the screen, X, to another, Y, and back to X. In contrast, we base our analysis on counting movements from X to Y even if there is no return to X. In problems where the response time is relatively long, the two approaches yield the same qualitative results. In problems where the response time is relatively short, their method does not yield sufficient data to make significant inferences.
The lotteries $L = (x_1, p_1)$ and $R = (x_2, p_2)$ are compared.

<table>
<thead>
<tr>
<th></th>
<th>The lotteries</th>
<th>% of choices</th>
<th>$\alpha$-values</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$L = (3000, 0.15)$</td>
<td>$R = (4000, 0.11)$</td>
<td>35</td>
</tr>
<tr>
<td></td>
<td>$L = (1700, 0.4)$</td>
<td>$R = (1300, 0.5)$</td>
<td>35</td>
</tr>
<tr>
<td></td>
<td>$L = (637, 0.649)$</td>
<td>$R = (549, 0.732)$</td>
<td>41</td>
</tr>
<tr>
<td></td>
<td>$L = (13600, 0.31)$</td>
<td>$R = (15500, 0.27)$</td>
<td>35</td>
</tr>
</tbody>
</table>

Table 1: $\alpha$-values in lottery choice problems (estimates standard deviations are in parenthesis, bold percentages emphasize the difference in $\alpha$-values between a problem in which the expected payoff calculation is easy and one in which it is difficult).

Our first conclusion is drawn from the comparison of problems U1-U2 and problems U3-U4 which differ in the difficulty of calculating the expectation. For U3-U4 (which involves a difficult calculation) the average proportion of horizontal movements is 59-61% as compared to only 45-47% for U1-U2 (which involves an easy calculation). We infer that when the expectation calculation is relatively difficult participants tend to use a C-procedure.9

Our main interest is in the procedure used in problems like U1 and U2. In order to interpret the results, we compared them to results in two other types of problem in which the deliberation process is transparent.

In D1 and D2, participants were asked to indicate which difference is larger (a-b or c-d). Results are summarized in Table 2:

---

9 In order to determine whether there is a consistent tendency among some participants towards either horizontal (H) or vertical (V) eye movements, we calculated (V-H)/(V+H) for the 27 participants for whom there were reliable measures for all of U1-U4. To do so, we looked at the ranking of participants for each question separately. Using a non-parametric test, we compared the mean ranking of each participant over the four questions to the distribution of the mean of four uniformly sampled numbers. We found that only 1 out of the 27 participants had a mean rank that was significant at the 5% level (compared to 1.3 which would be expected by chance).
The differences \( \alpha \) values 

\[
L = a - b \\
R = c - d
\]

\[
N \%
\]

\[
\alpha - \text{values}
\]

<table>
<thead>
<tr>
<th></th>
<th>L = a - b</th>
<th>R = c - d</th>
<th>N</th>
<th>%L</th>
<th>%R</th>
<th>38%</th>
<th>44%</th>
<th>13%</th>
<th>3%</th>
<th>2%</th>
<th>1%</th>
</tr>
</thead>
<tbody>
<tr>
<td>D1</td>
<td>251 222</td>
<td>187 153</td>
<td>38</td>
<td>24%</td>
<td>76%</td>
<td>38%</td>
<td>44%</td>
<td>13%</td>
<td>3%</td>
<td>2%</td>
<td>1%</td>
</tr>
<tr>
<td>D2</td>
<td>983462 718509</td>
<td>983501 718499</td>
<td>37</td>
<td>22%</td>
<td>78%</td>
<td>18%</td>
<td>22%</td>
<td>35%</td>
<td>20%</td>
<td>3%</td>
<td>3%</td>
</tr>
</tbody>
</table>

Table 2: \( \alpha \)'s for problems in which differences were compared.

In D1, the most straightforward procedure involves computing the differences using vertical eye movements. And indeed, vertical eye movements accounted for 82% of the time spent on this problem. In D2, the easiest way of making the choice is to calculate horizontal differences and indeed the share of vertical eye movements declined to 40%. Figure 3 presents the eye movements of two typical participants; both of them used vertical eye movements almost exclusively in D1 while in D2 horizontal eye movements dominated.

Figure 3: Eye movements for two participants while responding to D1 (left two boxes) and D2 (right two boxes).

In T1, T2 and T3, participants were asked to choose between receiving a sum of money on a particular date and a different sum of money on another date. The results are summarized in Table 3.
The alternatives of choices \( \alpha \)-values

\[
L = (x_1, t_1) \quad R = (x_2, t_2)
\]

\[
N \%L \%R 16% (1%) 15% (1%) 24% (1%) 39% (2%) 3% (1%) 4% (1%)
\]

\[
T1 \quad \$351.02 \quad \$348.23 \quad 39 \quad 92% \quad 8%
\]

\[
T2 \quad \$467.39 \quad \$467.00 \quad 38 \quad 58% \quad 42%
\]

\[
T3 \quad \$500.00 \quad \$508.00 \quad 39 \quad 74% \quad 26%
\]

Table 3: \( \alpha \)'s for time preference problems. Experiments took place during June-September 2008.

In this case, it is hard to imagine that any of the participants made a "present-value-like" computation which would have involved vertical eye movements. Indeed, we found that 2/3 of eye movements were horizontal. Thus, participants clearly used a C-procedure; in other words, they based their decisions on comparing sums of money and delivery dates separately.

We are now ready to compare the eye movements in problems U1 and U2 with those observed in problems involving the comparison of differences (D1 and D2) and time preferences (T1, T2, T3). For convenience, in Figure 4 we present the \( \alpha \)-values of the participants in problem U1 alongside their \( \alpha \)-values in D1 and T3.

Table 3: \( \alpha \)'s for time preference problems. Experiments took place during June-September 2008.

Figure 4: \( \alpha \)'s (and \( \beta \)'s) for participants in U1, D1 and T3.
We find that $\alpha$-values in U1 and U2 fell in between those of the other two problems. The proportion of vertical eye movements in the problems involving choice under uncertainty were well below those in a problem like D1 and well above those in problems involving time preferences, such as T3, in which it is clear that participants use a C-procedure. In each of these problems, the distribution of the frequency of horizontal movements is relatively concentrated around the average. Therefore, we conclude that most participants in the lottery problems U1 and U2 use procedures that are largely, but not solely, based on the comparison of components.

In another group of problems, we switched the locations of the probability and the dollar amount on the right side of the screen (see Figure 5):

![Figure 5](image)

Figure 5: Choice under uncertainty problem: diagonal layout.

In all the problems apart from those in this group, the $\alpha$-values of the diagonal movements were negligible. In contrast, diagonal movements were used intensively here (see Table 4).

---

10 The distribution of the horizontal movements shows a single peak with standard deviation of 13%.
We conclude that participants are heavily involved in comparing prizes and probabilities separately when making the choice between two lotteries.

### 5. Conclusion

The aim of this study was to use eye tracking in order to shed light on the procedures used by decision makers in the context of decision making under uncertainty. We conclude that when the numbers which specify the prices and probabilities of two lotteries made the expectation calculation difficult, they rely almost exclusively on separate comparisons of prizes and probabilities. In the other cases, it appears that they are involved in a hybrid of C- and H-procedures.
Reference


